# Variables and data types

(\*) Data comes from *observations*.

(\*) Each observation yields values for one or more *variables*.

(\*) **Qualitative variables:** The characteristic is **categorical**. E.g., gender, ethnicity, treatment group vs. control group.

(\*) **Quantitative variables:** The characteristic is **numerical**. E.g., income level, age, blood pressure. Quantitative variables can be *discrete* or *continuous*.

- **Discrete** variables can take values that differ by fixed amounts, usually used to *count* things. E.g., number of children.
- Continuous variables can take values that differ by arbitrarily small amounts. E.g., height or temperature. Continuous variables come in two flavors. Interval variables the difference between two values has a reasonable interpretation, but the ratio does not. E.g., temperature. Ratio variables the ratio between two values has a reasonable interpretation. E.g., height.

**Example:** 500 households are surveyed by a marketing research firm. The investigators collect data on: size of each household; monthly household income; occupation of head-of-household ; number of computers in house; type of internet connection.

(\*) 500 observations, each producing data for five variables.

(\*) Household size, monthly income and number of computers — these are quantitative variables.

- Income is a continuous variable.
- Household size and number of computers are discrete variables.

(\*) Occupation of head of household and type of internet connection are qualitative variables.

### Tables – categorical data

(\*) Categorical data can be *summarized* in tables by recording the *frequency* or *relative frequency* of the data in each category.

**Example.** The table below describes the results of the randomized, doubleblind field test of the Salk polio vaccine.

Group	size	infections/100,00
Treatment	$200,\!000$	28
Control	$200,\!000$	71
No consent	$350,\!000$	46

(\*) Observations: children.

(\*) Variables: group to which child belongs (three categories) and infection status (two categories).

## Distribution tables – quantitative data

(\*) To summarize quantitative data in a table, the typical approach is to transform it into *categorical data* (sort of).

(\*) The *range* of the observed values is divided into *class intervals*, also called *bins*. The bins play the role of the categories.

(\*) The *frequency*, or *relative frequency* of each class interval is recorded in a *distribution table*.

- The frequency of a bin is the *number* of the observations that fall into that bin.
- The relative frequency of a bin is the *proportion* of the observations that fall into that bin. Proportions are typically recorded as *percentages*.

**Comment:** Data can be divided into class intervals in different ways. How this is done can affect the way that the data is perceived.

Example:	US household	incomes from	12015 -	frequency	distribution.
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Income level	Frequency
\$0 - \$14,999	$14,\!595,\!004$
15,000 - 24,999	$13,\!210,\!995$
\$25,000 - \$34,999	$12,\!581,\!900$
\$35,000 - \$49,999	$15,\!979,\!013$
\$50,000 - \$74,999	$21,\!011,\!773$
\$75,000 - \$99,999	$15,\!224,\!099$
\$100,000 - \$149,999	$17,\!740,\!479$
\$150,000 - \$199,999	$7,\!800,\!778$
200,000  and over	$7,\!674,\!959$

Example:	US	household	incomes	from	2015 -	relative	frequency	distribution.
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Income level	Relative frequency
\$0 - \$14,999	11.6%
\$15,000 - \$24,999	10.5%
\$25,000 - \$34,999	10%
\$35,000 - \$49,999	12.7%
\$50,000 - \$74,999	16.7%
\$75,000 - \$99,999	12.1%
\$100,000 - \$149,999	14.1%
\$150,000 - \$199,999	6.2%
200,000  and over	6.1%

**Comment:** A distribution table makes it much easier to absorb large amounts of data. The price we pay is the loss of information inherent in *summarizing*.

When determining the class intervals for the table, you have to decide how much of the fine detail you are willing to lose.

And what message you are trying to convey.

Income level	Relative frequency
\$0 - \$24,999	22.1%
\$25,000 - \$49,999	22.7%
\$50,000 - \$99,999	28.8%
\$100,000 and over	26.4%

## **Cross-tabulation**

(\*) In studies with more than one category (or more than one quantitative variable), we can produce different distribution tables for different categories. The separate distribution tables can be combined into one table (with many columns).

(\*) The result of this process is called a *cross-tabulation*, and it helps to *control for* (observe the effect of) confounding variables.

**Example.** Oral contraceptives and blood pressure. The following table summarizes the results of the study on the effects of oral contraceptives on the blood pressure of women who use them done by the Kaiser clinic in Walnut Creek, CA.

- (\*) Qualitative variable: user/nonuser
- (\*) Quantitative variable: *blood pressure*.
- (\*) Variable controlled for: *age*.

Table 2. Systolic blood pressure by age and pill use, for women in the Contraceptive Drug Study, excluding those who were pregnant or taking hormonal medication other than the pill. Class intervals include the left endpoint, but not the right. – means negligible. Table entries are in percent; columns may not add to 100 due to rounding.

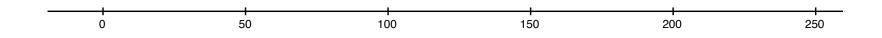
Blood	Age I	Age 17–24		Age 25–34		Age 35–44		Age 45–58	
pressure (millimeters)	Non- users	Users	Non- users	Users	Non- users	Users	Non- users	Users	
	(%)	(%)	(%)	(%)	(%)	(%)	(%)	(%)	
under 90		1	1	b <del>a se</del>	1	1	1		
90-95	1	_	1		2	1	1	1	
95-100	3	1	5	4	5	4	4	2	
100-105	10	6	11	5	9	5	6	4	
105–110	11	9	11	10	11	7	7	7	
110–115	15	12	17	15	15	12	11	10	
115-120	20	16	18	17	16	14	12	9	
120-125	13	14	11	13	9	11	9	8	
125-130	10	14	9	12	10	11	11	11	
130–135	8	12	7	10	8	10	10	9	
135–140	4	6	4	5	5	7	8	8	
140–145	3	4	2	4	4	6	7	9	
145-150	2	2	2	2	2	5	7	9	
150-155	_	1	1	1	1	3	2	4	
155-160			<u> </u>	1	1	1	1	3	
160 and over					1	2	2	5	
Total percent	100	98	100	99	100	100	99	99	
Total number	1,206	1,024	3,040	1,747	3,494	1,028	2,172	437	

### Histograms

A *histogram* is a graphical representation of a distribution table (for quantitative data).

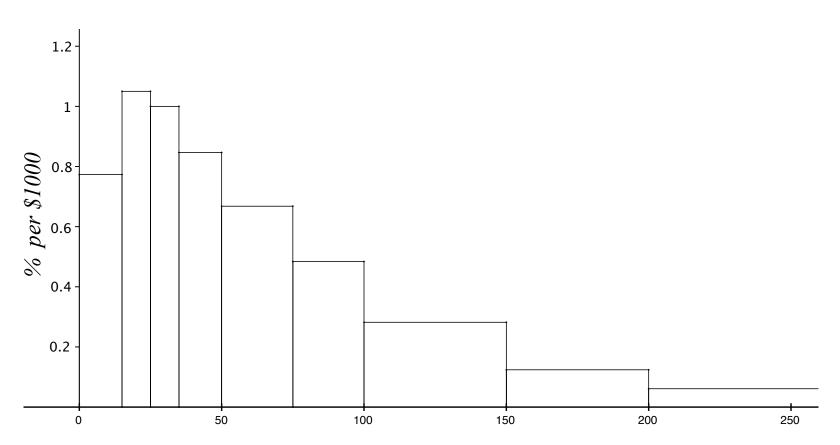
- Histograms *for data* are usually drawn as bar-charts.
- The horizontal axis of the chart is divided into class intervals.
- The scale on the vertical axis of the chart is typically one of following three:
- (\*) The frequency the number of all observations in a given bin.
- (\*) The *relative frequency* the percentage of all observations in a given bin.
- (\*) The density the relative frequency of the bin divided by its width.
  - If one uses the *density scale* (as we will be in this class), then the *area* of the region drawn above a class interval represents the *relative frequency* of (pecentage of data in) that class interval.

**Example:** Starting with the table of income distribution we saw earlier, we first draw the horizontal axis...



... Using a density scale, we draw rectangles over each class interval whose areas equal the percentages of the families in those intervals.

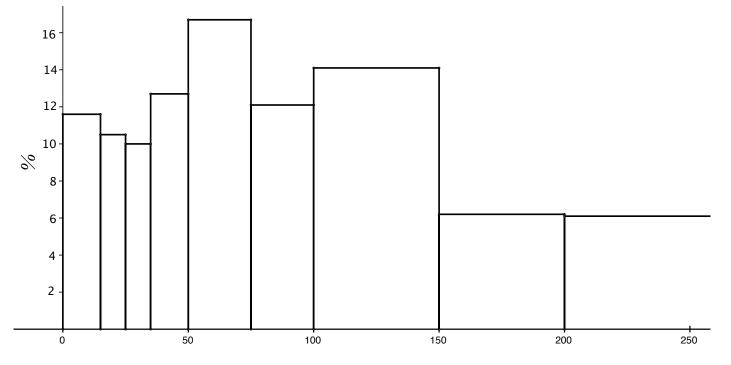
The height of each rectangle is equal to the percentage of the observations in the corresponding class interval divided by the length of the class interval (the width of the rectangle). The end-result should look like this



2015 U.S. Household Income (\$1000s)

The vertical scale here is *percent per* \$1000 - i.e., it is the relative frequency (percentage) divided by the width of the intervals (which in this case are measured in \$1000s). It's always a good idea to label the axes.

If, for example, we use the *relative frequency* scale instead of the *density* scale, the histogram looks like this:



2015 U.S. Household Income (\$1000s)

This histogram reports the information accurately, but it is misleading. The bins for the higher incomes seem to be much bigger than the bins for the lower incomes *because they are wider*.

(\*) If bins have different widths — use the density scale.

**Comment:** If all the bins in the distribution table have the same width, then the appearance of the histogram will be the same for all three scales. Only the units (and numbers) on the vertical scale will change.

**Example:** Distribution of coal (by weight) in Christmas stockings of 40 children at Wool's orphanage.

ounces of coal	number of stockings
0 - 5	2
5 - 10	4
10 - 15	8
15 - 20	8
20 - 25	10
25 - 30	4
30 - 35	4

